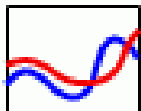


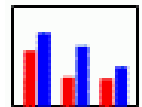
# An Error Decomposition Method: Application to Mediterranean SST simulations assessment.

Z. Ben Bouallegue, A. Alvera-Azcarate, J.-M. Beckers.  
GHER, University of Liege, Belgium

***International Verification Methods Workshop***



*September 15-17, 2004, Montreal*



# Mediterranean Forecasting System : Toward Environmental Predictions



## OGCM

- . 3D primitive equation
- . Z coordinates
- . Horizontal resolution  $1/8^\circ.1/8^\circ$
- . 31 vertical levels

## Simulations

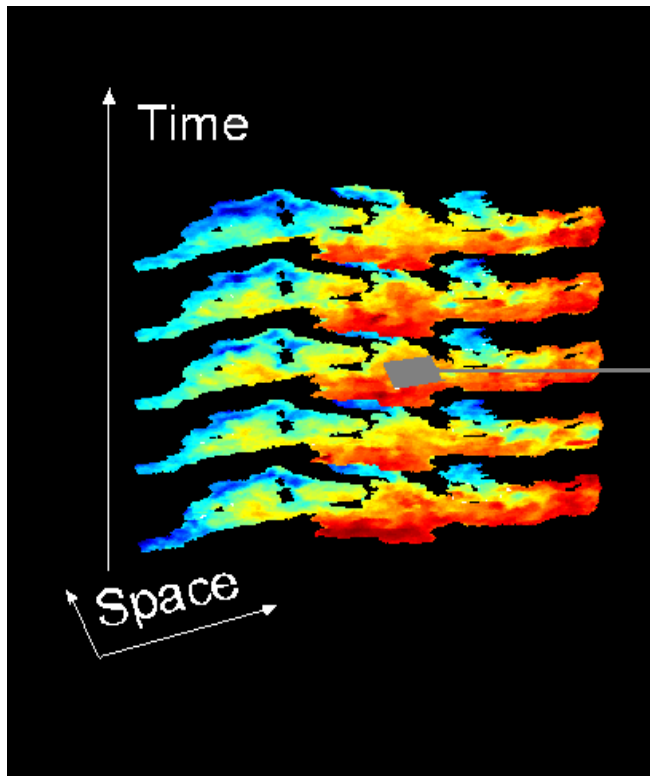
- . Forecast : 10 days
- . Assimilation each week
- . Forcing : Rigid lid, Atlantic box, Heat fluxes from atmospheric fields

Realized in the **INGV** of Bologna : [www.bo.ingv.it](http://www.bo.ingv.it)

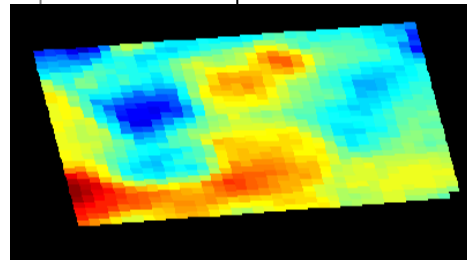
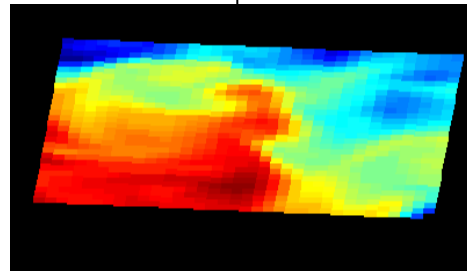
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# Assessment of the Sea Surface Temperature : The problematic

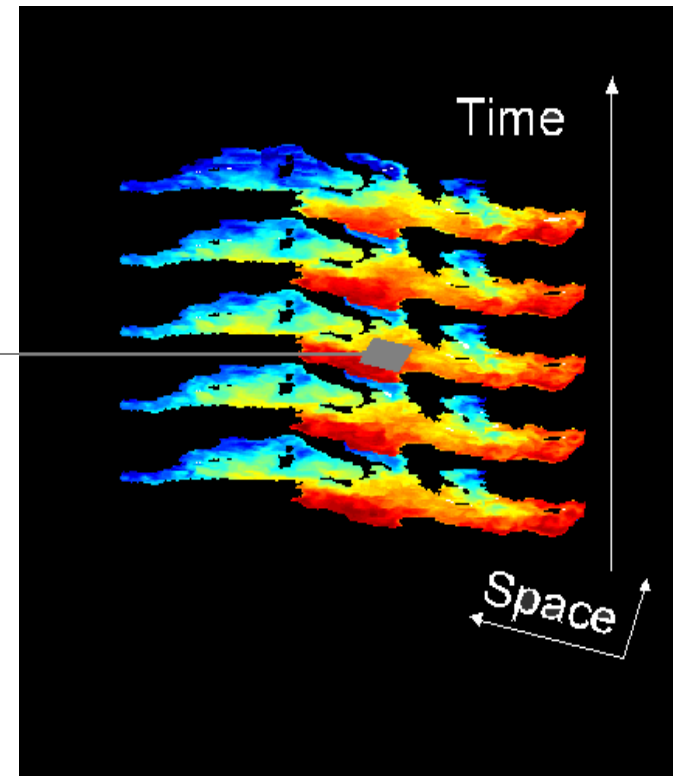
## Simulations



## Comparison



## Observations



**Snap shot view : no spatial or temporal context**

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# Assessment of the Sea Surface Temperature : The Mean Square Error

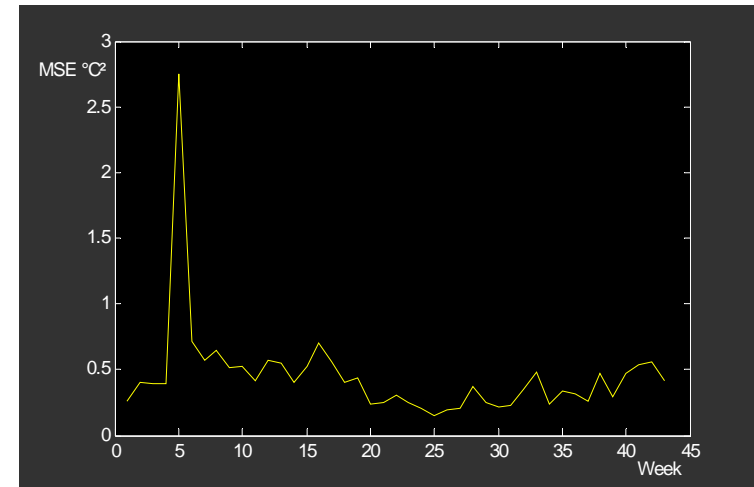
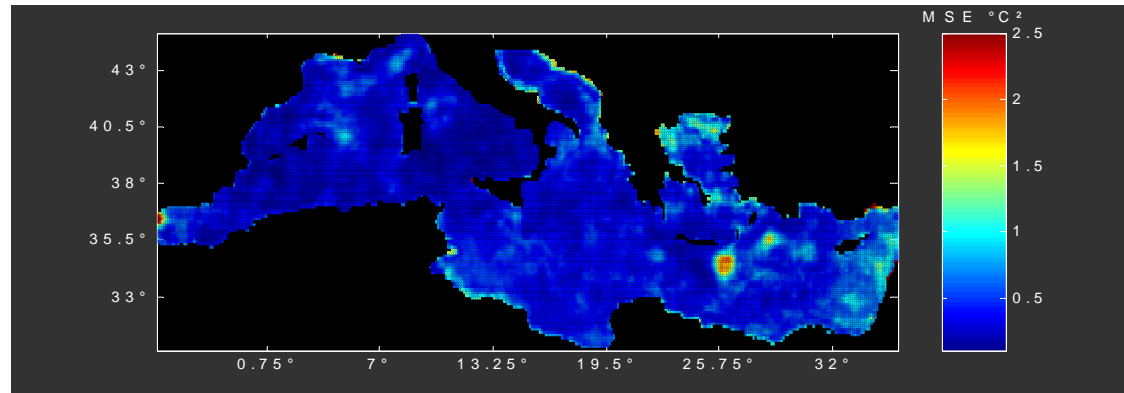
$$\text{MSE} = \overline{[(S - O)^2]}$$

O : Satellite observations  
available every week

S : Simulations from the OGCM

Hindcasts  $H_i$  are provided every days  
Hindcasts = Forecast + assimilation

$$S = \left( \sum_{i=D1}^{D7} H_i \right) / 7$$



Period: September 1999 – August 2000    Region: the whole Mediterranean Basin

# Error Decomposition Method (EDM) : the principle

*Inspired by 'E. E. Ebert and J. L. McBride 2000'.*

- $$\text{MSE} = \overline{[ (S(i,j,t) - O(i,j,t))^2 ]}$$

where S : Simulations ,

O : Observations

i , j : grid points

t : weeks

- Parameters optimization

$J$  the temporal shift,

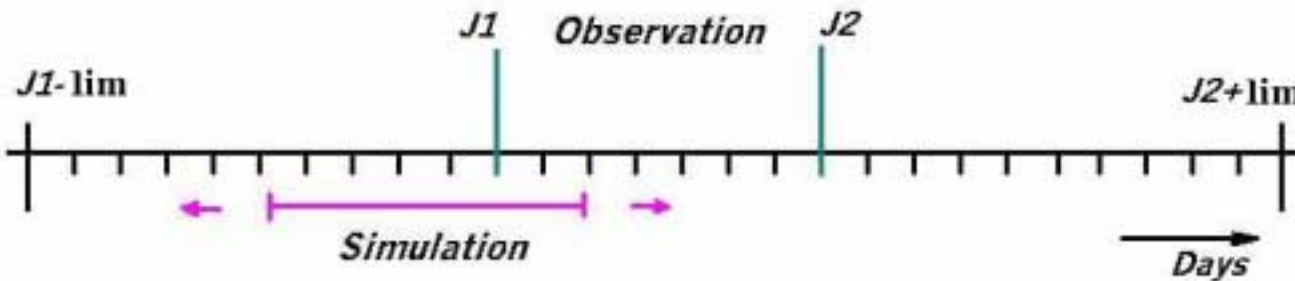
$(d_x, d_y)$  the bi-dimensional translation,

$T_i$  the bias

minimizing the Mean Square Error

- $$\text{MSE} = \text{MSE}_{\text{Trs Time}} + \text{MSE}_{\text{Trs Space}} + \text{MSE}_{\text{Intensity}} + \text{MSE}_{\text{pattern}}$$

- Evaluation of the time positioning parameter  $J$  and of its corresponding error



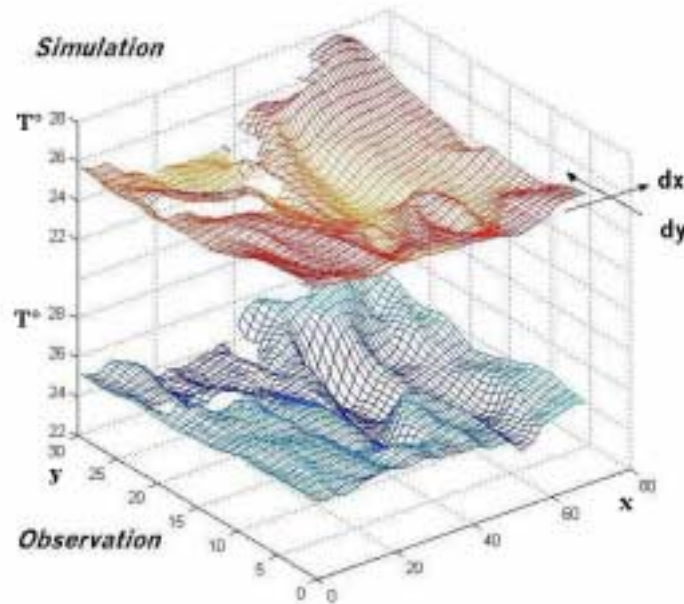
Translation in time:  $J \in [J1 - \text{lim}, J1 + \text{lim}]$  as

$$\text{MSE}_{M1} = \overline{\{ [ S(i,j,t+J) - O(i,j,t) ]^2 \}} \text{ is minimum}$$

$$\text{MSE}_{\text{Trs time}} = \text{MSE}_O - \text{MSE}_{M1}$$

## Error Decomposition Method (EDM) : 2<sup>nd</sup> step

- Evaluation of the space positioning parameters ( $dx$  ,  $dy$ ) and of it corresponding error



Translation in space:  $(dx, dy) \in [-2, +2]$  as

$$MSE_{M2} = \{ [ S(i+dx, j+dy, t) - O(i,j,t) ]^2 \} \text{ is minimum}$$

$$MSE_{Trs \text{ space}} = MSE_{Trs \text{ time}} - MSE_{M2}$$

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- Evaluation of the intensity parameters  $T_i$  and of its corresponding error

Intensity:  $T_i$  as

$$MSE_{M3} = \overline{\{ [ S(i, j, t) - O(i, j, t) + T_i ]^2 \}} \quad \text{is minimum}$$

$$MSE_{Intensity} = MSE_{Trs\ space} - MSE_{M3}$$

- Evaluation of the pattern error

Pattern:

$$MSE_{Pattern} = MSE_O - MSE_{Trs\ time} - MSE_{Trs\ space} - MSE_{Intensity}$$



- $$\text{MSE} (i,j,t) = \sum_{\text{t}}^{\text{T. Domain}} \sum_{\text{i}} \sum_{\text{j}}^{\text{S. Domain}} \left( S (i,j,\mathbf{t}+\mathbf{J}) - O (i,j,t) \right)^2 / (L_s.L_s.L_t)$$

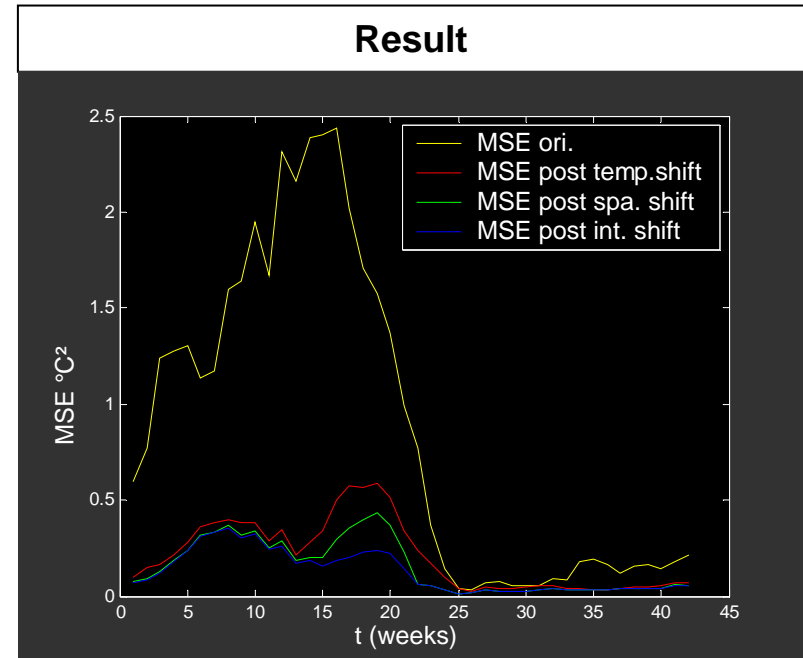
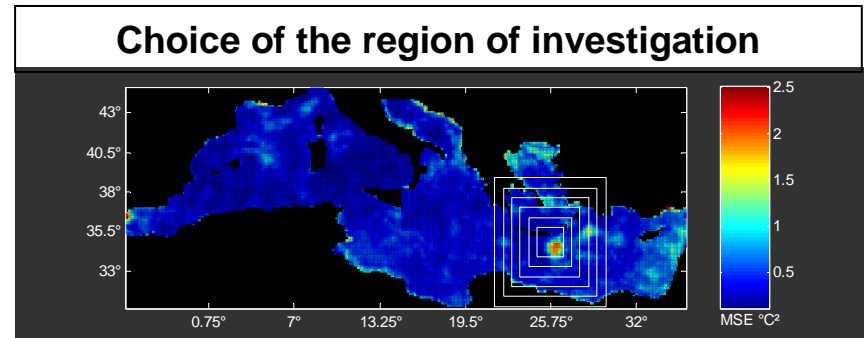
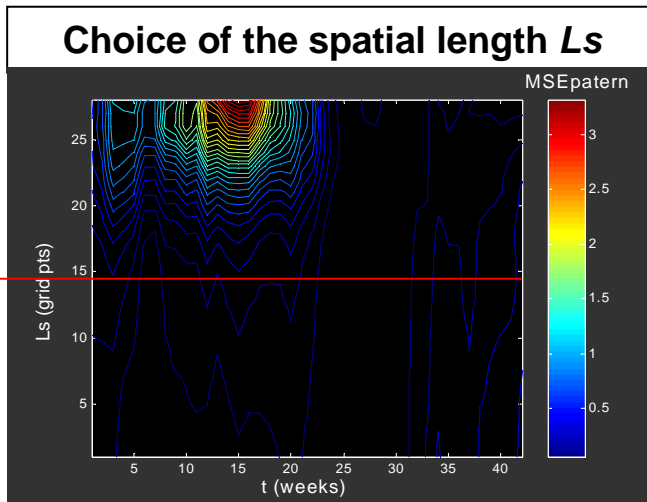
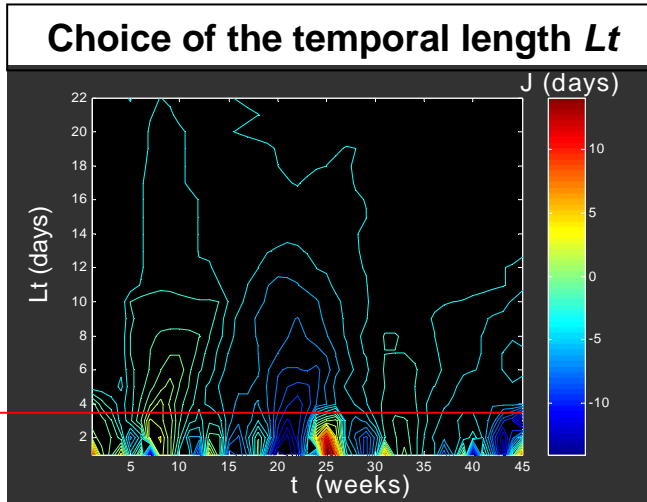
- $$\text{MSE} (i,j,t) = \sum_{\text{i}} \sum_{\text{j}}^{\text{S. Domain}} \left( S (\mathbf{i}+\mathbf{dx},\mathbf{j}+\mathbf{dy},t) - O (i,j,t) \right)^2 / (L_s.L_s)$$

- $$T_i = \sum_{\text{i}} \sum_{\text{j}}^{\text{S. Domain}} \left( S (i,j,t) - O (i,j,t) \right) / (L_s.L_s)$$

where  $L_t$  is the length of the time domain (nbr of weeks used)  
 $L_s$  is the length of the space square domain (nbr of grid pts)

# Error Decomposition Method (EDM) : Application 1

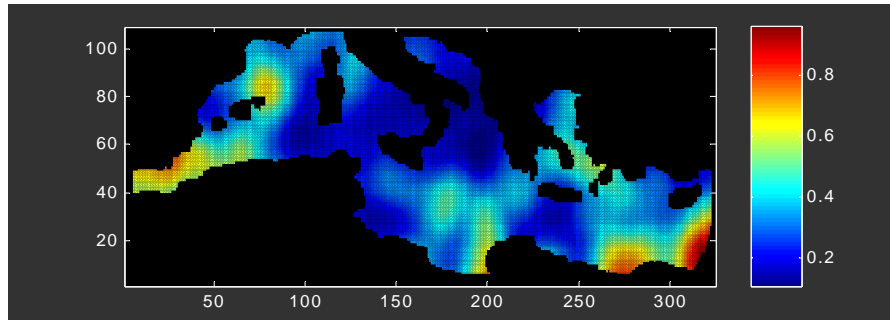
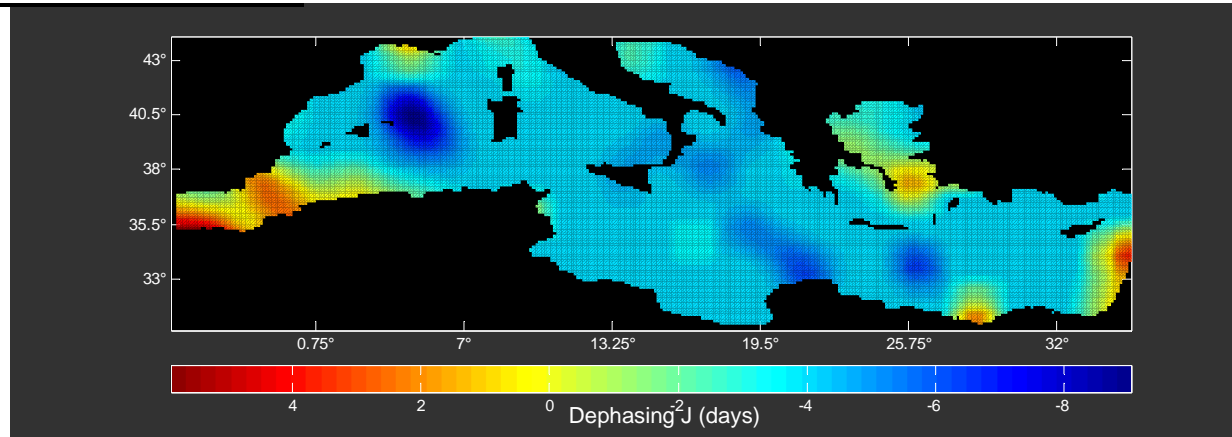
## Local analyze (Step by step analysis)



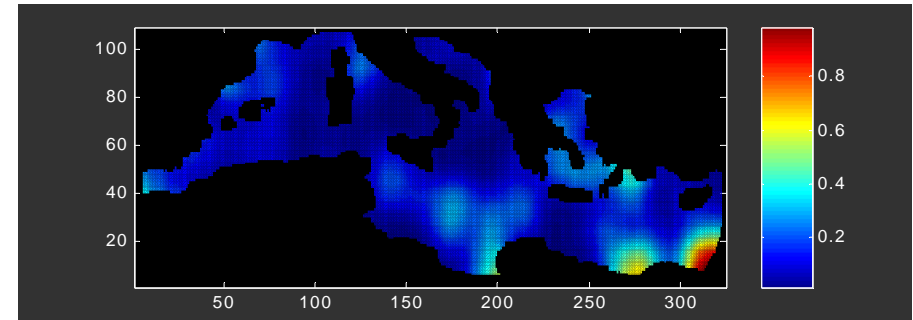
## Global analyze (one by one analysis)

1<sup>st</sup> week of October, spatial length **Ls=14** (1.75°,160 km) , time length **Lt =5** days

### Translation in time



MSE original ( $^{\circ}\text{C}^2$ )

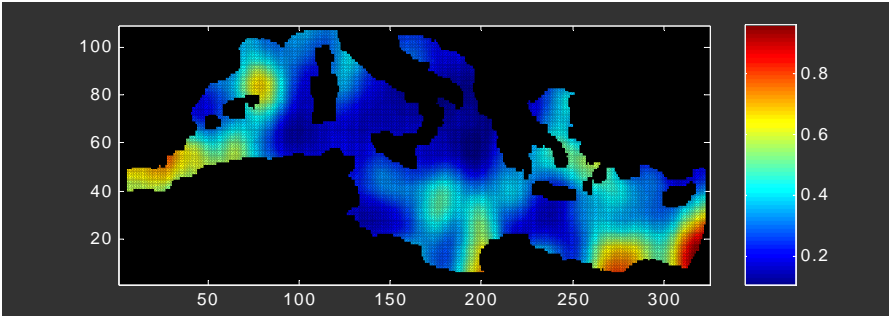
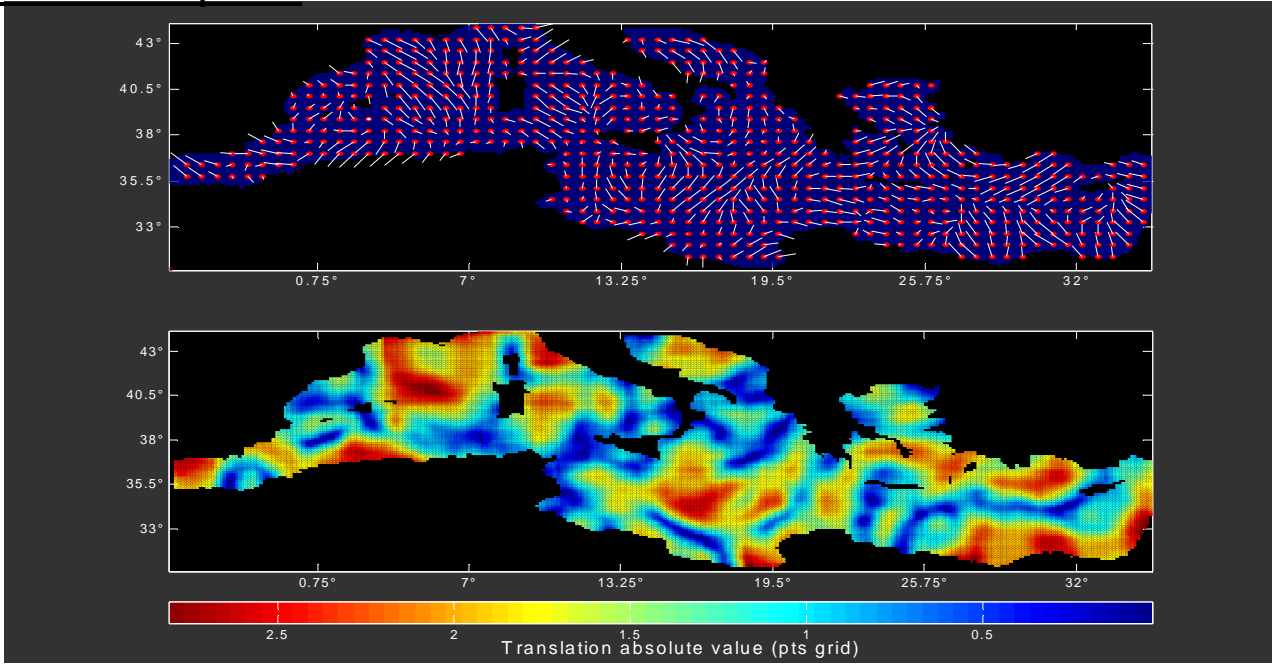


MSE post temporal trans. ( $^{\circ}\text{C}^2$ )

**Gain : 58% MSE resolved**

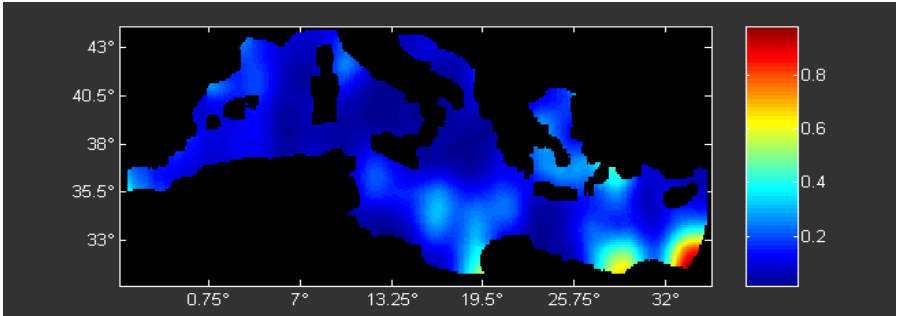
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## Translation in space



MSE original (°C²)

Gain : 25% MSE resolved



MSE post spatial trans. (°C²)

- Analyze of the parameters themselves

- Correlation Type – Source of the errors

*Temporal shift*

- Forcing : filtering
- Assimilation : synopticity

*Intensity shift*

- Forcing : bias
- Missing information

*Spatial shift*

- Bathymetry : discretization
- Parameterization

*Pattern error*

- Parameterization : turbulence
- Model discretization

- Solution of the double penalty

Comparison of MSE<sub>Pattern</sub>

**E. E. Ebert, \_ and J. L. McBride 2000.**

**‘Verification of precipitation in weather systems: determination of systematic errors’**

**Bureau of Meteorology Research Centre, Melbourne, Vic., Australia**

**Thank you for your attention**

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